

## Feathers, Keys and Splines

### 1) Feathers:

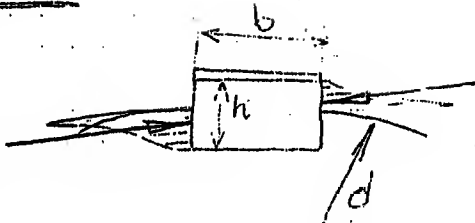
$$b = \frac{d}{4} + (2 \rightarrow 5) \text{ mm}$$

to get even no

$$h = \frac{b}{2} + (2-3) \text{ mm}$$

to get even no

$$(b = 0.25 - 0.3 d)$$



For  $\phi 50$

$\phi 75$	$b = 18.75 + 3.25 = 22$ $h = 11 + 2 = 13 \text{ mm}$
$\phi 120$	$b = 30 + 2 = 32$ $h = 16 + 2 = 18$

$$b = \frac{50}{4} + 3.5 = 16$$

$$h = \frac{16}{2} + 2 = 10$$

$$b \times h = 16 \times 10$$

Fit on sides, H/k fit (called keying fit)

Material St. 60 ( $\sigma_y = 30 \text{ kg/mm}^2$ )

( $\tau_y \approx 20 \text{ kg/mm}^2$ )

Length:-

Fixed { Calculated for crushing in hub (usually C1)  
Checked for shear.

Sliding { common length in contact calculated for bearing pressure & checked for shear.

$$\tau_{all} \leq \frac{2T}{bdL} \quad \text{i.e.} \quad L \geq \frac{2T}{bd\tau_{all}}$$

For the shaft:

$$\tau_{all} \geq \frac{16T}{\pi d^3} \quad \text{i.e.} \quad L \geq \frac{2T(\pi d^3)}{bd(16T)}$$

$$\pi \approx 3, \quad b \approx \frac{d}{4}$$

$$\therefore L \geq \frac{4 \times 2 \times 3 d^2}{16 \times d} \geq 1.5 d$$

This length is based on equality of allowable shear stress of key & shaft.

Allowable Stresses:

1- Crushing :-

$$\frac{\sigma_y}{2} \text{ of the weakest material}$$

$$(800 - 1500 \text{ kg/cm}^2)$$

C.I.      C.St

higher allowable values are accepted for steady running & light overloads.

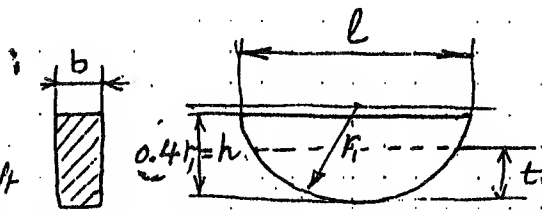
2- Bearing pressure :-

Sliding at low speed and under load

$$p = 100 - 200 \text{ kg/cm}^2$$

2- Woodruff Key:

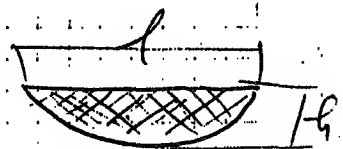
$$b = 0.15 - 0.2 d_{\text{shaft}}$$



if  $t (\approx 0.6h)$  is more than  $\frac{1}{3} d_{\text{sh}}$ , use another connection

Calculated mainly for crushing in the hub. Widely used in automotive industries. Usually used to transmit part of the power transmitted by the shaft.

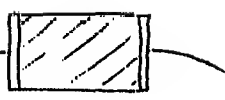
$$l = (0.92 \rightarrow 0.98) d$$



$$\text{Area} = \frac{h}{6s} (3h^2 + 4s^2)$$

### 3) Taper keys:

- Saddle
- On flat
- Sunk

Tangential keys 

Taper 1:100 metric &  $\frac{1}{8}$ " per foot in English systems which is equivalent to 1:96

Sunk key:

$$T \leq Qa + \mu Qc + \mu N \frac{d}{2}$$

let  $c \approx 0.5d$

$$a = \frac{b}{6}$$

$$N = \frac{4}{\pi} Q$$

&  $Q = 0.5 b l \sigma_{cr}$   
distribution factor  $\sigma_{cr}$

$$\therefore T \leq Q \left[ a + \mu c + \frac{2\mu d}{\pi} \right]$$

$$\leq \frac{bl}{2} \left[ \frac{b}{6} + \frac{\mu d}{2} + \frac{2\mu d}{\pi} \right] \sigma_{cr} \quad N = \frac{4}{\pi} Q$$

$$\leq \frac{bl}{12} \left[ b + 3 \left( 1 + \frac{4}{\pi} \right) \mu d \right] \sigma_{cr}$$

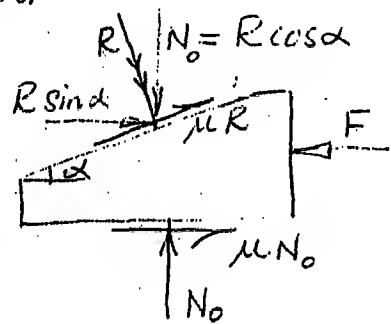
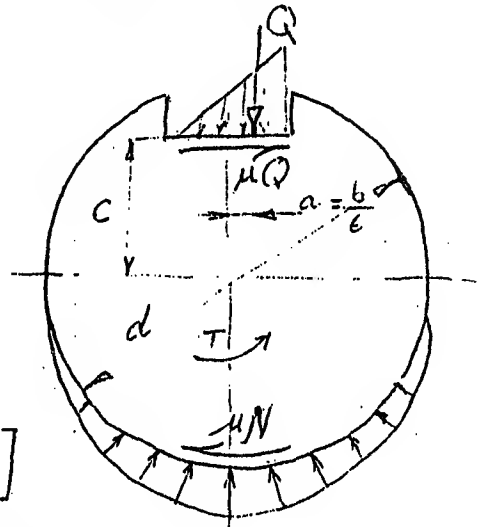
Driving force:

$$F = \mu N_0 + R \sin \alpha + \mu R \cos \alpha$$

$$= \mu N_0 + N_0 \frac{\sin \alpha}{\cos \alpha} + \mu N_0$$

$$= N_0 \left[ \tan \alpha + 2\mu \right], \quad N_0 = Q$$

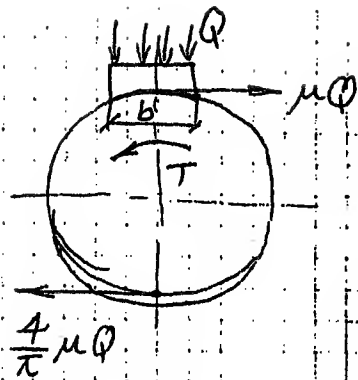
$$Q = N_0 = \frac{T}{\left[ a + \mu c + \frac{2\mu}{\pi} d \right]}$$



### Saddle key:

$$T \leq \mu Q \frac{d}{2} \left[ 1 + \frac{4}{\pi} \right]$$

$$\text{i.e. } T \leq \mu Q \frac{d}{2} (2.28) \\ \leq 1.14 \mu Q d$$



l by check for crushing with hub:

$$\sigma_{cr} \leq \frac{Q}{b l} \quad \text{i.e. } l \geq \frac{Q}{b \sigma_{cr}}$$

### Key on flat:-

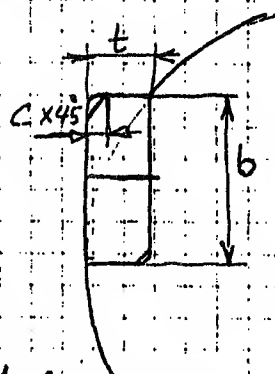
The same as the sunk key.

### Tangential keys:

$$T \leq Q \frac{d-t}{2} + \frac{4}{\pi} \mu Q \frac{d}{2}$$

$$\text{let } t \cong 0.1 d, Q \leq (t-c) l \sigma_{cr}$$

$$\therefore T \leq \left( 0.145 + \frac{2\mu}{\pi} \right) d l (t-c) (\sigma_{cr})$$



Two sets in opposite position  $120^\circ$  apart to allow for transmission in two directions of rotation.

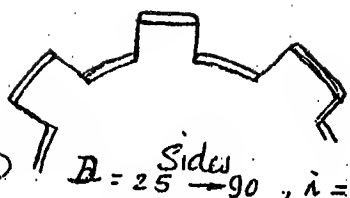
In heavy duty  $t = 0.1 d$   
 $b = 0.3 d$   
 Std key joints  
 $t = 0.115 d \rightarrow 0.066 d$   
 $b = 0.32 d \rightarrow 0.248 d$   
                     ↓                    ↓  
                   small 'd'      large 'd'

## 4) Splines

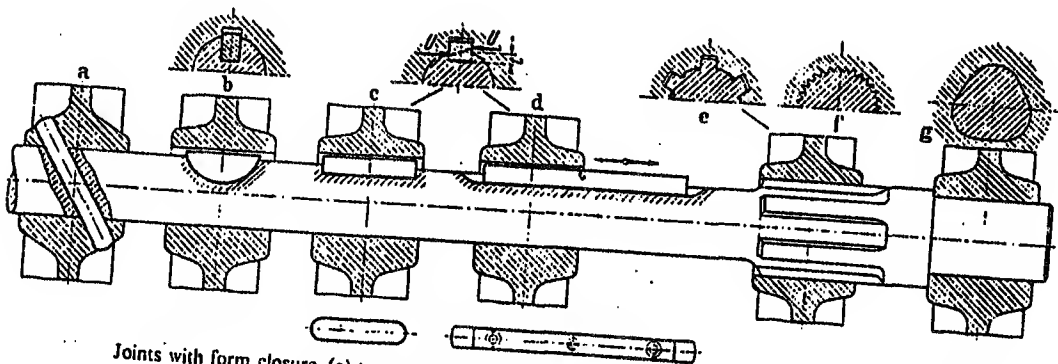
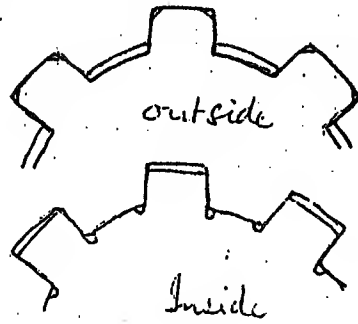
### 4-1- Parallel sides

less accu., high Capacity

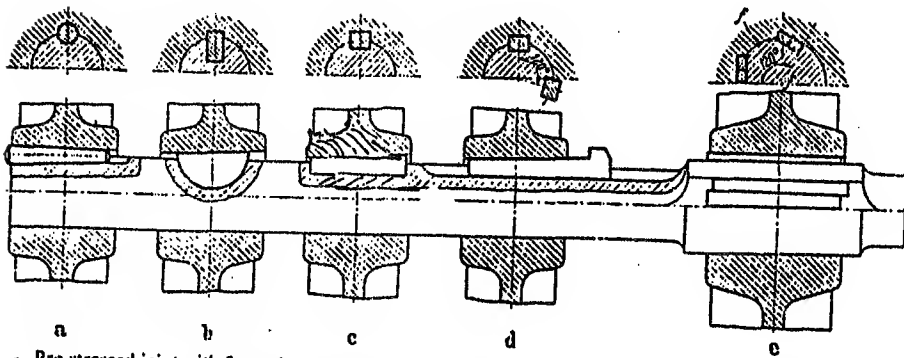
- Fit on sides
- Fit on outside  $D$
- Fit on inside  $d$



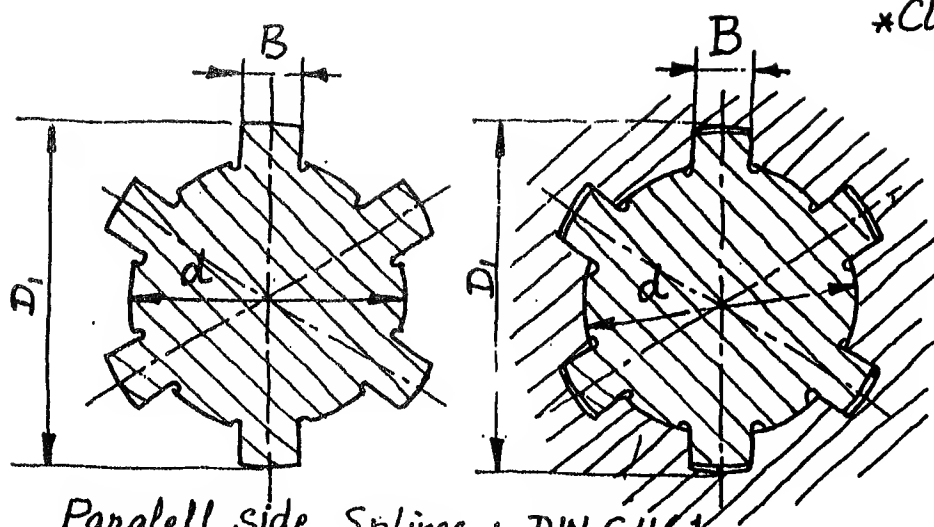
$$B = \frac{\text{Sides}}{25} \rightarrow 90, \lambda = 10$$



Joints with form closure, (a) transverse pin, (b) woodruff key, (c) laid in feather key (parallel key), (d) sliding feather key, (e) splined profile, (f) serrated tooth profile, (g) K-profile.



Pre-stressed joint with form closure, (a) round taper key (end key), (b) tapered woodruff key, (c) sunk taper key, (d) driven taper key with or without gth head (at 120° to each other if two keys are used), (e) tangential key (f-f = position of parting line) when the hub is split.



\*Class of Fit on  $d$  :

- For light series :

$H_7/f_7$

- For Medium series :

$H_7/g_7$

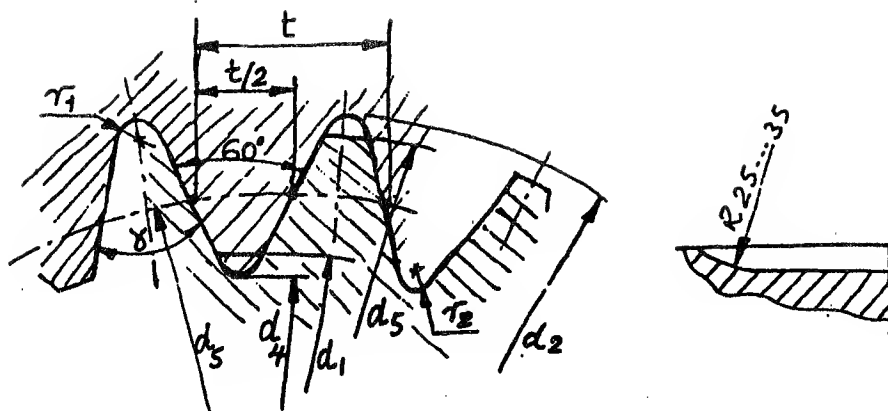
- For Heavy series :

$H_7/h_7$

\* For other tolerances  
in details, see  
DIN 5465

Parallel Side Splines : DIN 6461

Inner $d$	No of Splines	Light Series DIN 5462		Medium Series DIN 5463		No of Splines	Heavy Series DIN 5464	
		$D_1$	$B$	$D_1$	$B$		$D_1$	$B$
16	6			20	4	10	20	2.5
18				22	5		23	3
21				25	5		26	3
23		26	6	28	6		29	4
26		30	6	32	6		32	4
28		32	7	34	7		35	4
32	8	36	6	38	6		40	5
36		40	7	42	7		45	5
42		46	8	48	8		52	6
46		50	9	54	9		56	7
52		58	10	60	10	12	60	5
56		62	10	65	10		65	5
62		68	12	72	12		72	6

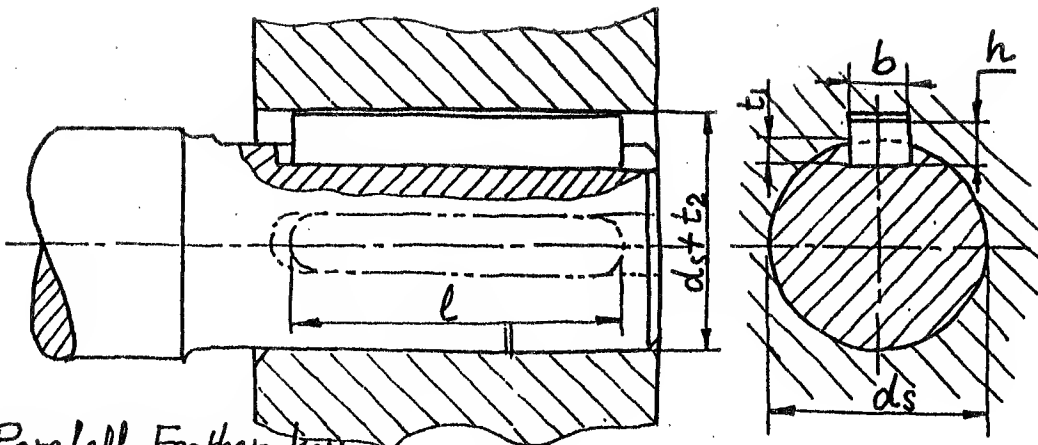


Serrations , DIN 5481

$(d_1 \times d_3)$ $\phi$	$d_1$ (An)	$d_2$	$d_3$ (An)	$d_4$	$d_5$	$r_1$ $\approx$	$t$ (measured on $d_5$ )	$Z$
10 x 12	10.1	12	12	10.2	11	0.1	1.152	30
12 x 14	12	14.18	14.2	12.06	13	0.1	1.317	31
15 x 17	14.9	17.28	17.2	14.91	16	0.15	1.571	32
17 x 20	17.3	20	20	17.37	18.5	0.15	1.761	33
21 x 24	20.8	23.76	23.9	20.76	22	0.15	2.033	34
26 x 30	26.5	30.06	30	26.40	28	0.25	2.513	35
30 x 34	30.5	34.17	34	30.38	32	0.3	2.792	36
36 x 40	36	40.16	39.9	35.95	38	0.5	3.226	37





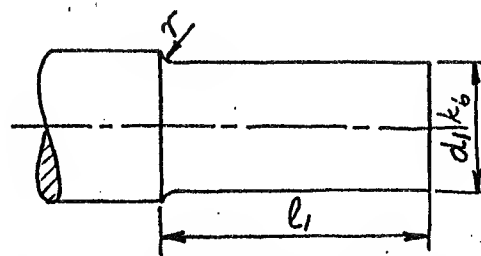
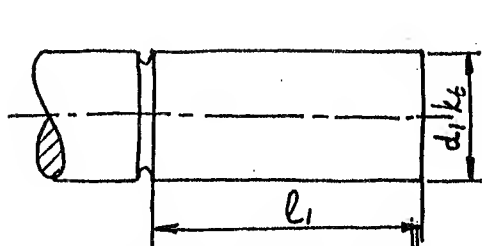


Parallel Feather key:

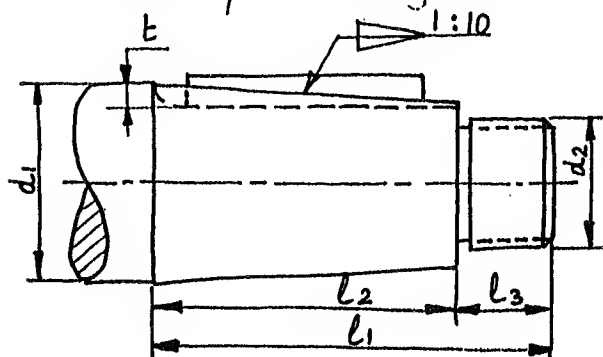
(Extracted From DIN 6885 Table 1)

$d_s$		$b$	$h$	$t_1$	$t_2$	$l$	
From	Up to					From	Up to
6	8	2	2	1.2	1	6	20
8	10	3	3	1.8	1.4	6	36
10	12	4	4	2.5	1.8	8	45
12	17	5	5	3	2.3	10	56
17	22	6	6	3.5	2.8	14	70
22	30	8	7	4	3.3	18	90
30	38	10	8	5	3.3	22	110
38	44	12	8	5	3.3	28	140
44	50	14	9	5.5	3.8	36	160
50	58	16	10	6	4.3	45	180
58	65	18	11	7	4.4	50	200
65	75	20	12	7.5	4.9	56	210
75	85	22	14	9	5.4	63	250
85	95	25	14	9	5.4	70	280
95	110	28	16	10	6.4	80	320

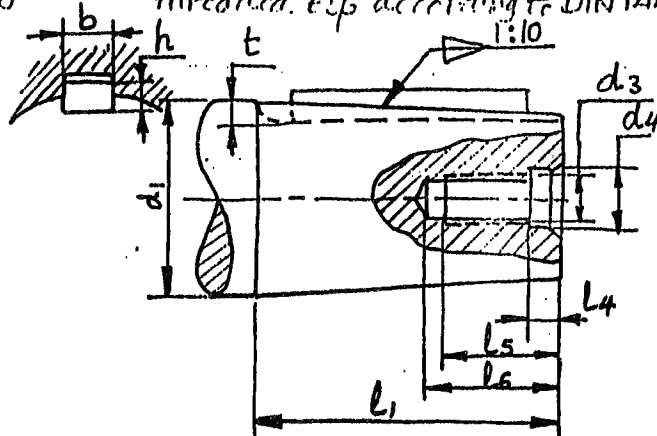
\* Cylindrical shaft ends according to DIN 748-1



\* Tapered shaft end with externally threaded tip according to DIN 1448

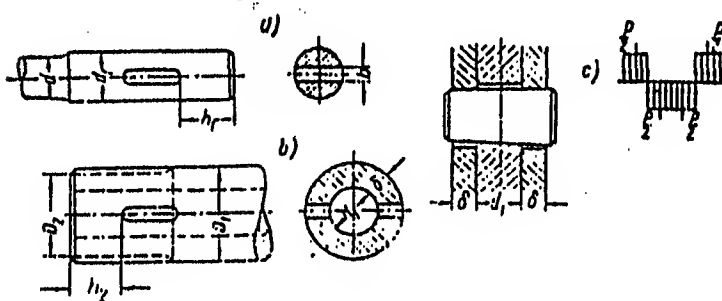
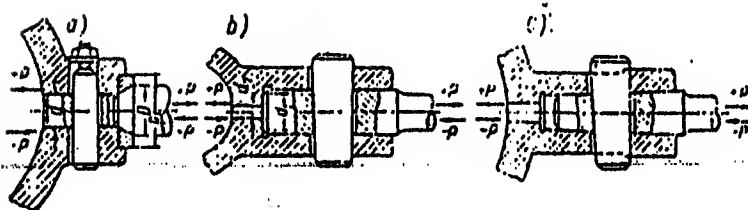
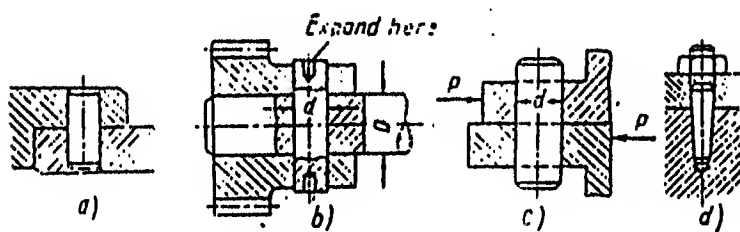
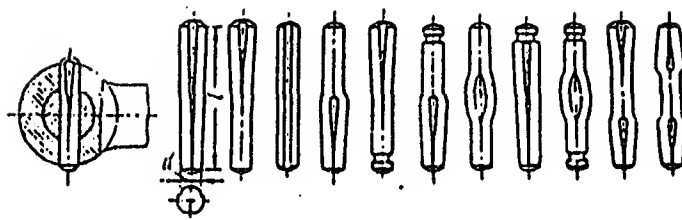
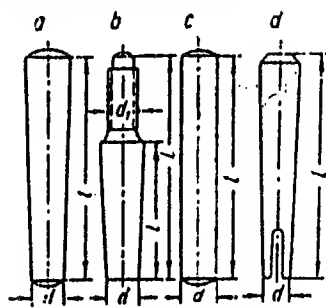


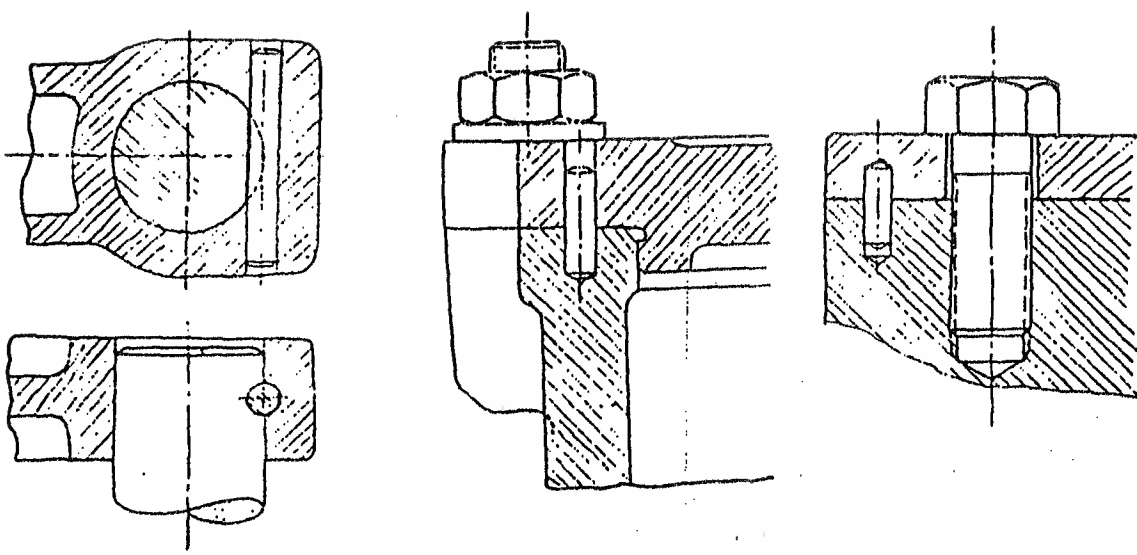
\* Tapered shaft end with internally threaded tip according to DIN 1449



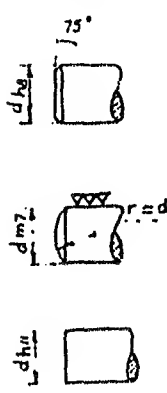
$d_1$	$l_1$		$l_2$		$l_3$	$l_4$	$l_5$	$l_6$	$r$	$t$		$b \times h$	$d_2$	$d_3$	$d_4$
	Long	Short	Long	Short						Long	Short				
12										1.7	—	2x2			
14	30	18	18	—						2.3	—	3x3	M8x1	M4	4.3
16					12	3.2	10	14		2.5	2.2				
19	40	28	28	16		4	12.5	17	0.6	3.2	2.9		M10x1.25	M5	5.3
20															
22	50	36	36	22	14	5	16	21		3.4	3.1	4x4	M12x1.25	M6	6.4
24										3.9	3.6				
25															
28	60	42	42	24	18	6	19	25		4.1	3.6	5x5	M16x1.5	M8	8.4
30										4.5	3.9				
32						7.5	22	30					M20x1.5	M10	10.5
35	80	58	58	36	22				1	5	4.4	6x5			
38															
40						9.5	28	37.5				10x8	M24x2	M12	13
42															
45	110	82	82	54	28					7.1	6.4		M30x1		
48						12	36	45				12x8		M16	17
50									1.6				M36x3		

# Pins and Cotters

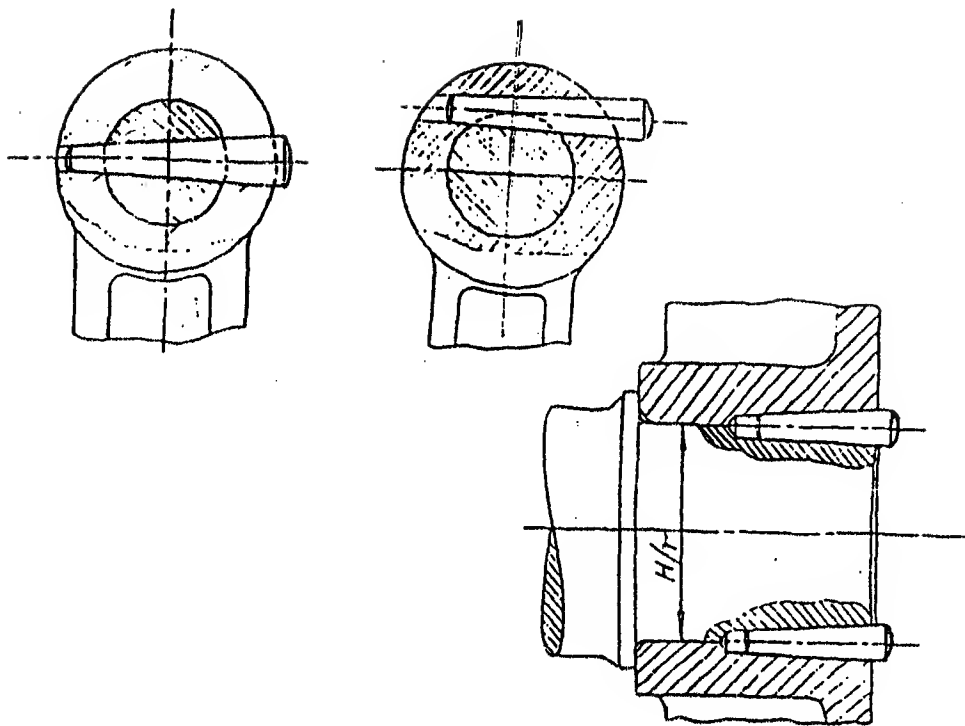




# PARALLEL PINS



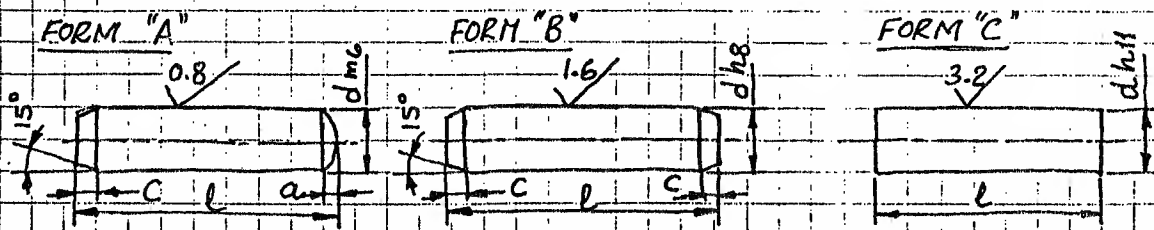
d	L																a
2	5	6	8	10	12	14	16	18	20	22	25	28	30	32	35	38	0,4
3	8	10	12	14	16	18	20	22	25	28	30	32	35	38	40	45	0,5
4	10	12	14	16	18	20	22	25	28	30	32	35	38	40	45	50	0,6
5	12	14	16	18	20	22	25	28	30	32	35	38	40	45	50	55	1
6	14	16	18	20	22	25	28	30	32	35	38	40	45	50	55	60	1
8	16	18	20	22	25	28	30	32	35	38	40	45	50	55	60	65	1,5
10	18	20	22	25	28	30	32	35	38	40	45	50	55	60	65	70	1,5
12	20	22	25	28	30	32	35	38	40	45	50	55	60	65	70	75	1,5
14	22	25	28	30	32	35	38	40	45	50	55	60	65	70	75	80	1,5
16	25	28	30	32	35	38	40	45	50	55	60	65	70	75	80	85	1,5
18	28	30	32	35	38	40	45	50	55	60	65	70	75	80	85	90	2,5
20	30	32	35	38	40	45	50	55	60	65	70	75	80	85	90	95	2,5
22	32	35	38	40	45	50	55	60	65	70	75	80	85	90	95	100	2,5
25	35	38	40	45	50	55	60	65	70	75	80	85	90	95	100	105	2,5
28	38	40	45	50	55	60	65	70	75	80	85	90	95	100	105	110	2,5



TAPER PINS

d	r	L																			
1	1,5	8	10	12	14	16	18	20	22	25											
1,5	1,5		10	12	14	16	18	20	22	25											
2	2,5			12	14	16	18	20	22	25	28	30	32	35							
2,5	2,5			12	14	16	18	20	22	25	28	30	32	35	38	40					
3	4				14	16	18	20	22	25	28	30	32	35	38	40	45	50			
4	4					16	18	20	22	25	28	30	32	35	38	40	45	50	55	60	
5	6						20	22	25	28	30	32	35	38	40	45	50	55	60	70	
6	6	25	28	30	32	35	38	40	45	50	55	60	70	80	90	100					
8	10		28	30	32	35	38	40	45	50	55	60	70	80	90	100	110	120	130	140	
10	10				32	35	38	40	45	50	55	60	70	80	90	100	110	120	130	140	
13	15	38	40	45	50	55	60	70	80	90	100	110	120	130	140	150	165	180	200	220	
16	20		40	45	50	55	60	70	80	90	100	110	120	130	140	150	165	180	200	220	
20	20				50	55	60	70	80	90	100	110	120	130	140	150	165	180	200	220	
25	30					55	60	70	80	90	100	110	120	130	140	150	165	180	200	220	
30	30						60	70	80	90	100	110	120	130	140	150	165	180	200	220	

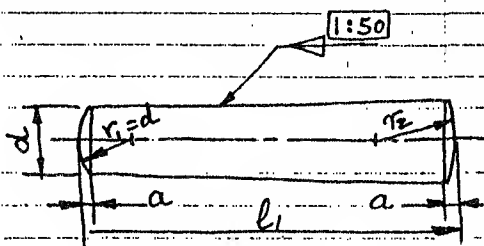
# Cylindrical Pins DIN EN ISO 2338



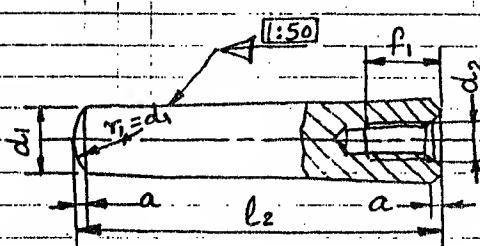
ISO 2338-A-5x20-St.

$\phi d$	1.2	1.5	2	2.5	3	4	5	6	8	10	12	16
$l$ [	4 12	4 16	6 20	6 24	8 32	8 40	10 50	12 60	14 80	18 95	22 140	26 180

## DIN EN 22339 Taper Pins



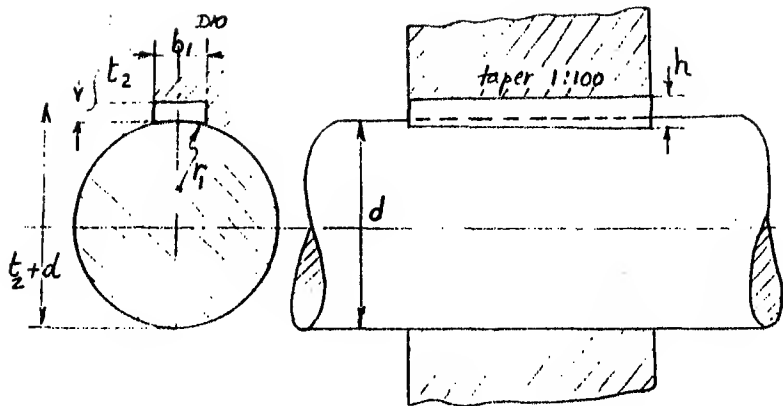
## DIN EN 28736



$\phi d/h_{10}$	1.5	2	2.5	3	4	5	6	8	10	12	16	20	25
$a$	0.2	0.25	0.3	0.4	0.5	0.6	0.8	1	1.2	1.6	2	2.5	3
$l_1$ [	8 24	10 35	10 35	12 45	14 55	18 60	22 90	22 120	25 150	32 180	40 200	45 200	50 200

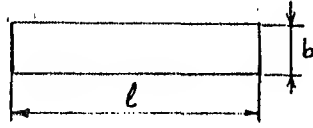
$$r_2 = \frac{a}{2} + d + \frac{(0.02 l)^2}{8a}$$

d	b	h	l
22 30	8	3.5	20 90
30 38	10	4	25 110
38 44	12	4	32 140
44 50	14	4.5	40 160
50 58	16	5	45 180
58 65	18	5	50 200
65 75	20	6	56 220
75 85	22	7	63 250



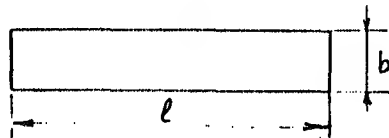
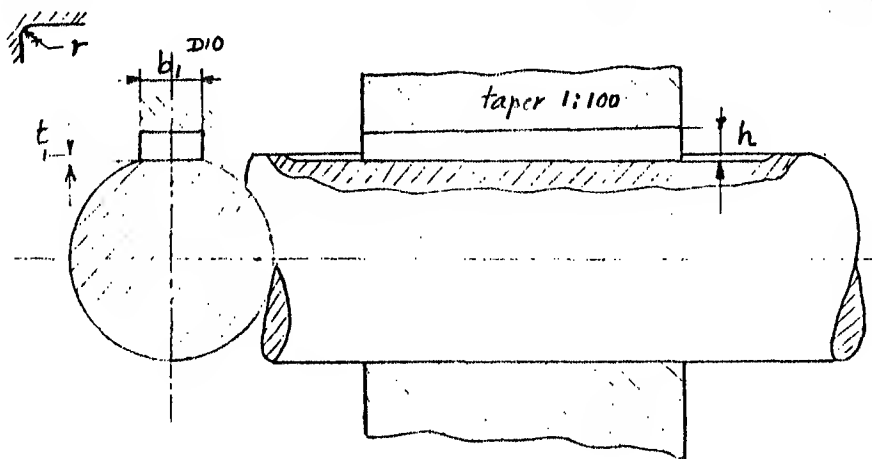
Saddle key

DIN 6881  
d > 22 ... 150 mm



l = 20, 22, 25, 28, 32, 36, 40, 45, 50, 56, 63, 70, 80, 90, 100, 110, 125, 140, 160, 180, 200, 220, 250, 280, 315

d	t1	t2	r1/r
22 30	1.3	3.2	15/0.4
30 38	1.8	3.7	19/0.4
38 44	1.8	3.7	22/0.5
44 50	1.4	4	25/0.5
50 58	1.9	4.5	29/0.5
58 65	1.9	4.5	33/0.5
65 75	1.9	5.5	38/0.6
75 85	1.8	6.5	43/0.6



Key on flat

DIN 6881  
d > 22 ... 230 mm

Mat. St. 60

Key size (b x h x l)

# Rivets dimensions according to DIN 660 , DIN 661

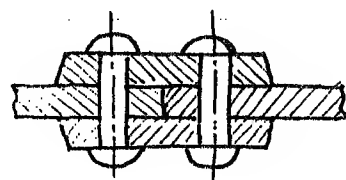
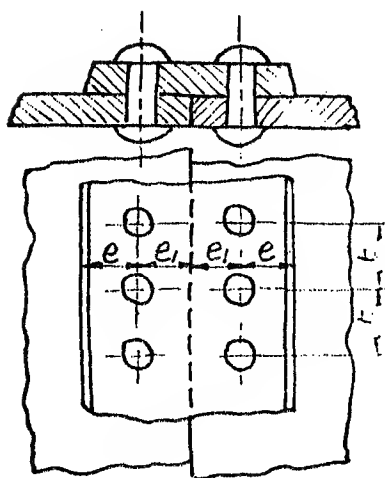
Neck diam.	$d_1$	1	1.2	(1.4)	1.6	2	2.5	3	3.5	4	5	6	(7)	8
Head diam	$d_2$	1.8	2.1	2.4	2.8	3.5	4.4	5.2	6.2	7	8.8	10.5	12.2	14
Min. tip diam	$d_3$	0.93	1.13	1.33	1.52	1.87	2.37	2.87	3.37	3.87	4.82	5.82	6.82	7.76
Neck Length	$e$	0.5	0.6	0.7	0.8	1	1.3	1.5	1.8	2	2.5	3	3.5	4
Through hole diam	$d_{H12}$	1.05	1.25	1.45	1.65	2.1	2.6	3.1	3.6	4.2	5.2	6.3	7.3	8.4
Button headed rivet	$d_8$	1.8	2.1	2.4	2.8	3.5	4.4	5.2	6.2	7	8.8	10.5	12.2	14
	$k_1$	0.6	0.7	0.8	1	1.2	1.5	1.8	2.1	2.4	3	3.6	4.2	4.8
	$r_1 \approx$	1	1.2	1.4	1.6	1.9	2.4	2.8	3.4	3.8	4.6	5.7	6.6	7.5
Countersunk headed rivet	$d_8$	1.8	2.1	2.4	2.8	3.5	4.4	5.2	6.2	7	8.8	10.5	12.2	14
	$k_2 \approx$	0.4	0.5	0.6	0.7	0.8	1	1.3	1.4	1.9	2.4	2.8	3.3	3.9
	$t_1$	0.4	0.5	0.6	0.7	0.8	1	1.3	1.4	1.8	2.3	2.7	3.2	3.7

Protruding length =  $\Delta l$

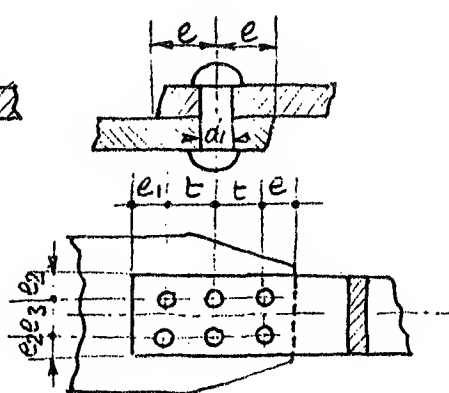
- Form A ,  $\Delta l = 1.8 d$  i.e  $l \geq s + 1.8 d$
- Form B ,  $\Delta l = 1.5 d$  i.e  $l \geq s + 1.5 d$

Std. Lengths:

2, 3, 4, 5, 6, 8, 10, 12, 14, 16, 18, 20, 22, 25, 28, 30, 32, 35, 38, 40



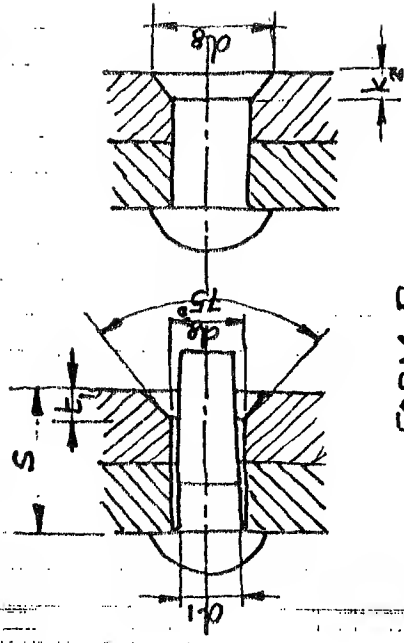
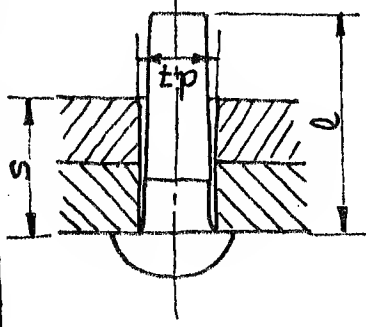
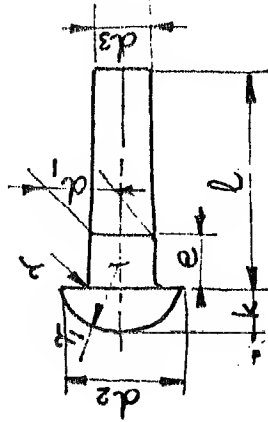
$$\begin{aligned}
 t &= 3.0 - 3.5 d_1 \\
 e_1 &= 2.0 - 2.5 d_1 \\
 e_2 &= 1.5 - 2.0 d_1 \\
 e_3 &= 3.0 - 3.5 d_1
 \end{aligned}$$





Button headed rivet

DIN 660

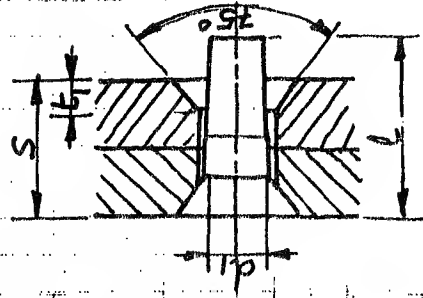
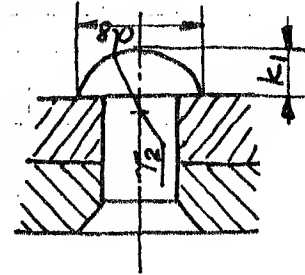
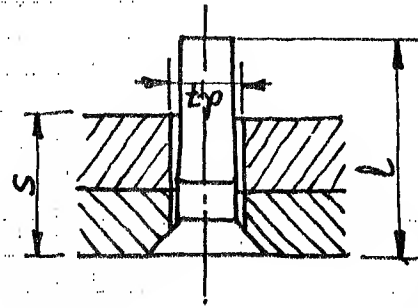
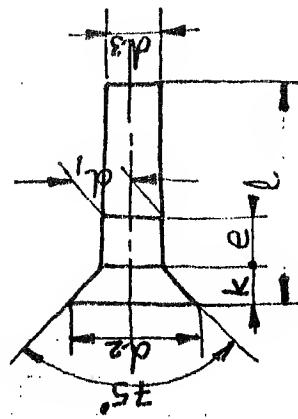


FORM A

FORM B

Countersunk headed rivet DIN 661 (July 1977)

135.



FORM A

FORM B